

# Matematiikan perusmetodit/mat.

## Harjoitus 12 syksy 2010

### A osa:

1. Integroi

a)  $\int \frac{1}{1+a^2x^2} dx$ , b)  $\int \frac{dx}{2+x^2}$ , c)  $\int \frac{x^2}{x^2+1} dx$ .

2. Integroi

a)  $\int x \sin x dx$ , b)  $\int x^2 \sin x dx$ , c)  $\int (2x + 1) \sin 2x dx$ .

3. Integroi

a)  $\int x e^{-\frac{x}{2}} dx$ , b)  $\int x^2 e^{2x} dx$ , c)  $\int x^3 e^x dx$ .

4. Integroi

a)  $\int \ln x^2 dx$ , b)  $\int x^2 \ln x dx$ , c)  $\int \frac{\ln(1+x^2)}{x^2} dx$ .

5. Integroi

a)  $\int \arctan x dx$ , b)  $\int \arcsin x dx$ .

6. Integroi

a)  $\int \cos(\ln x) dx$ , b)  $\int e^x \cos x dx$ .

7. Integroi

a)  $\int \frac{x}{x+\sqrt{x}} dx$ , b)  $\int \frac{1}{1+\sqrt{x-1}} dx$ , c)  $\int \frac{1}{1+\sqrt[3]{x+1}} dx$ , d)  $\int \frac{x}{(3x-1)\sqrt{3x-1}} dx$ .

8. Integroi

a)  $\int \frac{dx}{x(x-1)}$ , b)  $\int \frac{1+x^2}{x(1+x)} dx$ .

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### B osa:

#### 1. Integroi

a)  $\int \frac{1}{\sqrt{9-x^2}} dx$ , b)  $\int \frac{1}{\sqrt{x+\sqrt[3]{x}}} dx$ , c)  $\int \sqrt{2-x^2} dx$ , d)  $\int \frac{4^x+1}{2^x+1} dx$ ,  
f)  $\int \sqrt{x^2+2} dx$ .

#### 2. Integroi

a)  $\int \frac{x^2+7x}{(x-1)(x+1)^2} dx$ , b)  $\int \frac{5x-4}{(x+2)(x^2+3)} dx$ , c)  $\int \frac{x+1}{x^2-x+1} dx$ .

#### 3. Johda osittaisintegroinnin avulla palautuskaavat

a)  $\int \sin^n x dx = -\frac{1}{n} \sin^{n-1} x \cos x + \frac{n-1}{n} \int \sin^{n-2} x dx$ ,  $n = 2, 3, \dots$ ,

b)  $\int \cos^n x dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x dx$ ,  $n = 2, 3, \dots$